



18. What is the greatest number of the following five statements about numbers a, b which can be true at the same time?

$$\frac{1}{a} < \frac{1}{b}$$

$$a^2 > b^2$$

$$a < b$$

$$a < 0$$

$$b < 0$$

A 1

B 2

C 3

D 4

E 5

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18. **D** It is not possible for all five statements to be true at the same time since if $a < b, a < 0, b < 0$ are all true then $\frac{1}{a} < \frac{1}{b}$ is not true since $\frac{1}{b} - \frac{1}{a} = \frac{a-b}{ab}$ which is negative. However, when these three statements are true, $a^2 > b^2$ is also true, so it is possible for four of the statements to be true at the same time.