**Hypothesis Testing with the Normal Distribution Exam Questions**

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| The length of a train journey from Norwich to Ipswich follows a normal distribution with a mean of 45 minutes and a standard deviation of 10 minutes.  Commuters have complained in recent weeks that journeys are taking longer. A random sample of 36 journeys is taken, which is found to have a mean time of 48 minutes.   1. Test at the 5% significance level whether there is evidence of an increase in the train journey time. 2. Using the context of the problem, comment on the suitability of the journey times following a normal distribution. |  | The ages of members of a large bowling club is modelled by a normal distribution with a, previously calculated, average age of 61.4 years and standard deviation of 7.5 years.  The club secretary is concerned about the ageing membership of the club so takes a random sample of 16 members and finds their mean age to be 65.0 years.   1. Carry out a hypothesis test **by finding the critical region** at the 5% significance level, to determine whether the mean age of club members has changed. 2. Comment on the likely number of members aged under 25, giving a numerical reason for your answer. |
| Scientists believe the mass of narwhals .  Fisherman Bob Mortimer thinks the mean mass of Narwhals isn’t 900kg and decides to catch 10 narwhals to test this.  Bob catches 10 Narwhals and conducts a hypothesis test at the 5% significant level. He rejects , concluding that there is evidence to suggest the mean mass of Narwhals isn’t 900kg.  What are the smallest and largest possible mean masses of Bob’s catch? | Stringo Balls, a brand of string, are meant to be sold in lengths of 2m and it is claimed that the lengths follow a normal distribution with mean 2m and standard deviation 0.2m. A trading officer inspects a random sample of 22 balls and finds that the sample has a mean length of 1.91m.  Test whether this provides evidence at the 2% significance level, that the mean is less than 2m. | In previous years, marks obtained by students at Top-Notch College have been modelled by a normal distribution with mean 65 and standard deviation 9.  Teachers are concerned that this year, students are, on average, underachieving so select a random sample of 35 students whose mean score is found to be 61.5.  Investigate the teacher’s suspicion at the 5% level. |

**Writing Frame**

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|  |  | Trains | Narwhals | Stringo Balls | Bowls | Top Notch |
| 1 | Define the variable |  |  |  |  |  |
| 2 | Write down the null and alternate hypotheses | H0:  H1: | H0:  H1: | H0:  H1: | H0:  H1: | H0:  H1: |
| 3 | What is the significance level? |  |  |  |  |  |
| 4 | Is it one or two tailed? |  |  |  |  |  |
| 5 | Probability of this sample occurring randomly? |  |  |  |  |  |
| 6 | Is this probability less than or greater than the significance level? |  |  |  |  |
| 7 | Accept or reject the null hypothesis? |  |  |  |  |
| 8 | Conclude and clarify in context |  |  |  |  |

**Writing Frame - answers**

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|  |  | Trains | Narwhals | Stringo Balls | Bowls | Top Notch |
| 1 | Define the variable | average train time NOR > IPW | average mass of narwhals | average length of ball of string | average age of bowling members | average marks obtained |
| 2 | Write down the null and alternate hypotheses | H0:  H1: | H0:  H1: | H0:  H1: | H0:  H1: | H0:  H1: |
| 3 | What is the significance level? | 5% | 5% | 2% | 5% | 5% |
| 4 | Is it one or two tailed? | One | Two | One | Two | One |
| 5 | Probability of this sample occurring randomly? |  | Smallest and largest mean masses are  896.9 to 903.1 |  | Regions at  and |  |
| 6 | Is this probability less than or greater than the significance level? | It’s less than | It’s less than | 65 is within the accept region | It’s less than |
| 7 | Accept or reject the null hypothesis? | Reject | Reject | Accept | Reject |
| 8 | Conclude and clarify in context | There is evidence to suggest that average train times are longer than 45 minutes | There is evidence to suggest that average sizes of Stringo balls are smaller than 2m | There is insufficient evidence to suggest that average ages of bowling club members has increased | There is evidence to suggest that students are underachieving |