**is Irrational**

1. Assume is rational, i.e.
2. Where is a fraction in lowest terms, i.e. cancelled down as far as possible - IMPORTANT
3. Square both sides…
4. Multiply up…
5. must be even since
6. And therefore is even
7. And therefore is even (because even x even = even)

*\*This itself needs proving before we should continue\**

1. And therefore can be written as 2 another number…
2. And therefore…
3. And therefore…
4. And therefore…
5. And therefore is also an even number.
6. And therefore and are both even and are both divisible by two, i.e. they have a common factor of 2.
7. But we’ve already stated that…

Where is a fraction in lowest terms, i.e. cancelled down as far as possible - IMPORTANT

1. So we have a contradiction.
2. And therefore, our original assumption must be wrong…

is NOT rational but is irrational.

1. We’ve proved by contradiction that is NOT rational.

 **is Irrational**

1. Assume is rational, i.e.
2. Where is a fraction in lowest terms, i.e. cancelled down as far as possible - IMPORTANT
3. Square both sides…
4. Multiply up…
5. must be multiple of 5 since
6. And therefore is a multiple of 5
7. And therefore is a multiple of 5 (because if is multiple of 5 then is multiple of 5)

*\*This itself needs proving before we should continue\**

1. And therefore can be written as 5 another number…
2. And therefore…
3. And therefore…
4. And therefore…
5. And therefore is also an even number.
6. And therefore and are both multiples of 5 and are both divisible by five, i.e. they have a common factor of 5.
7. But we’ve already stated that…

Where is a fraction in lowest terms, i.e. cancelled down as far as possible - IMPORTANT

1. So we have a contradiction.
2. And therefore, our original assumption must be wrong…

is NOT rational but is irrational.

1. We’ve proved by contradiction that is NOT rational.

Why doesn’t this argument work for etc.?

Here’s why this argument doesn’t work for etc.

For roots of non-square numbers…

1. If is a square number and multiple of 2 (even) then is multiple of 2 (even)

Both factors must be same, and therefore…

1. If is a square number and multiple of 5 then is multiple of 5

Both factors must be same, and therefore…

However, for square numbers…

1. If is a square number and multiple of 4 then is multiple of 4.

Counter example:

 (is a multiple of 4)

 (not a multiple of 4)

1. If is a square number and multiple of 9 then is multiple of 9.

Counter example:

 (is a multiple of 4)

 (not a multiple of 4)

With square numbers, the square root is distributed across both factors instead of appearing in its entirety, and repeated, in both factors.

Therefore, the proof breaks down. There is no contradiction, the assumption remains correct and the conjecture that was to be proven remains unproven.

**Intro Task**

1. is a multiple of 2. What can you say about the number ?
2. is a multiple of 5. What can you say about the number ?
3. is a multiple of any prime number. What can you say about the number ?
4. is a multiple of 4. What can you say about the number ?

Can you give an example (counter-example?) to support your ideas?

1. is a multiple of 9. What can you say about the number ?

Can you give an example (counter-example?) to support your ideas?

1. is a multiple of 8. What can you say about the number ?
2. is a multiple of 12. What can you say about the number ?
3. is a multiple of any non-square, non-prime number. What can you say about the number ?