

Core 4 Calculus Answers

2(a)	$\frac{dy}{dt} = \frac{-2}{t^2}$ $\frac{dx}{dt} = -4$ $\frac{dy}{dx} = \frac{dy}{dt} \cdot \frac{1}{\frac{dx}{dt}} = \frac{1}{2t^2}$	M1A1 m1 A1F	4	Use chain rule Follow on use of chain rule (if $f(t)$) Or eliminate t : M1 $y=f(x)$ attempt to differentiate M1A1 chain rule A1F reintroduce t follow on gradient (possibly used later)
(b)	$t = 2$ $m_T = \frac{1}{8}$ $x = -5$ $y = 2$ $y - 2 = \frac{1}{8}(x + 5)$ $x - 8y + 21 = 0$	B1F B1 M1 A1F	4	Their $(x, y), m$ Ft on (x, y) and m
(c)	$x - 3 = -4t$ $y - 1 = \frac{2}{t}$ $(x - 3)(y - 1) = -4t \times \frac{2}{t} = (-8)$	M1 M1 A1	3	PI Attempt to eliminate t AG convincingly obtained
Total			11	

6(a)	$\cos 2x = 2\cos^2 x - 1$	B1B1	2	
(b)	$\cos^2 x = \frac{1}{2}(\cos 2x + 1)$ $\begin{aligned} \frac{1}{2} \int_0^{\frac{\pi}{2}} \cos 2x + 1 \, dx &= \left[\frac{1}{4} \sin 2x + \frac{x}{2} \right]_0^{\frac{\pi}{2}} \\ &= \frac{\pi}{4} \end{aligned}$	M1 A1 A1	5	Attempt to express $\cos^2 x$ in terms of $\cos 2x$ Use limits. Ft on integer a .
Total			7	

5(a)	$x = 1, 5a^2 - a - 4 = 0$ $(5a+4)(a-1) = 0, a = 1$	M1 A1	2	condone y for a AG – be convinced, both factors seen or $a = -\frac{4}{5}$ or $1 \Rightarrow a = 1$ A0 for 2 positive roots (substitute $(1, 1) \Rightarrow 5 = 5$ no marks)
(b)	$\frac{dy}{dx} + 4$ $= 10xy^2 + 10x^2y \frac{dy}{dx}$ $x = 1, y = 1 \quad \frac{dy}{dx} + 4 = 10 + 10 \frac{dy}{dx}$ $\frac{dy}{dx} = -\frac{6}{9} = \left(-\frac{2}{3}\right)$ Alt (for last two marks) $\frac{dy}{dx} = \frac{10xy^2 - 4}{1 - 10x^2y}$	B1B1 M1 M1 A1 M1 A1 (M1)	7	(Ignore ' $\frac{dy}{dx} =$ ' if not used, otherwise loses final A1) attempt product rule, see two terms added chain rule, $\frac{dy}{dx}$ attached to one term only condone 5×2 for 10 two terms, or more, in $\frac{dy}{dx}$ CSO find $\frac{dy}{dx}$ in terms of x, y and substitute $x = 1, y = 1$ must be from expression with two terms or more in $\frac{dy}{dx}$
(c)	$(1,1) \Rightarrow \frac{10-4}{1-10} = -\frac{6}{9}$ $\frac{y-1}{x-1} = -\frac{2}{3}$ (OE)	(A1) B1F	1	ft on gradient ISW after any correct form
	Total		10	

