## Statistics 1 Probability Questions

2 Xavier, Yuri and Zara attend a sports centre for their judo club's practice sessions. The probabilities of them arriving late are, independently, $0.3,0.4$ and 0.2 respectively.
(a) Calculate the probability that for a particular practice session:
(i) all three arrive late; (1 mark)
(ii) none of the three arrives late;
(iii) only Zara arrives late.
(b) Zara's friend, Wei, also attends the club's practice sessions. The probability that Wei arrives late is 0.9 when Zara arrives late, and is 0.25 when Zara does not arrive late.

Calculate the probability that for a particular practice session:
(i) both Zara and Wei arrive late;
(ii) either Zara or Wei, but not both, arrives late.
(3 marks)

6 A housing estate consists of 320 houses: 120 detached and 200 semi-detached. The numbers of children living in these houses are shown in the table.

|  | Number of children |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | None | One | Two | At least <br> three | Total |
| Detached house | 24 | 32 | 41 | 23 | 120 |
| Semi-detached house | 40 | 37 | 88 | 35 | 200 |
| Total | 64 | 69 | 129 | 58 | 320 |

A house on the estate is selected at random.
$D$ denotes the event 'the house is detached'.
$R$ denotes the event 'no children live in the house'. $S$ denotes the event 'one child lives in the house'. $T$ denotes the event 'two children live in the house'. ( $D^{\prime}$ denotes the event 'not $D^{\prime}$.)
(a) Find:

| (i) $\mathrm{P}(D)$; | (1 mark) |
| :--- | :---: |
| (ii) $\mathrm{P}(D \cap R) ;$ | (1 mark) |
| (iii) $\mathrm{P}(D \cup T) ;$ | (2 marks) |
| (iv) $\mathrm{P}(D \mid R) ;$ | (2 marks) |
| (v) $\mathrm{P}\left(R \mid D^{\prime}\right)$. | (3 marks) |

(b) (i) Name two of the events $D, R, S$ and $T$ that are mutually exclusive. (1 mark)
(ii) Determine whether the events $D$ and $R$ are independent. Justify your answer.
(2 marks)
(c) Define, in the context of this question, the event:
(i) $D^{\prime} \cup T$; (2 marks)
(ii) $D \cap(R \cup S)$. (2 marks)

5 Dafydd, Eli and Fabio are members of an amateur cycling club that holds a time trial each Sunday during the summer. The independent probabilities that Dafydd, Eli and Fabio take part in any one of these trials are $0.6,0.7$ and 0.8 respectively.

Find the probability that, on a particular Sunday during the summer:
(a) none of the three cyclists takes part;
(b) Fabio is the only one of the three cyclists to take part;
(c) exactly one of the three cyclists takes part;
(d) either one or two of the three cyclists take part.

2 The British and Irish Lions 2005 rugby squad contained 50 players. The nationalities and playing positions of these players are shown in the table.

|  |  | Nationality |  |  |  |
| :---: | :--- | :---: | :---: | :---: | :---: |
|  |  | English | Welsh | Scottish | Irish |
| Playing <br> position | Forward | 14 | 5 | 2 | 6 |
|  | Back | 8 | 7 | 2 | 6 |

(a) A player was selected at random from the squad for a radio interview. Calculate the probability that the player was:
(i) a Welsh back;
(1 mark)
(ii) English;
(2 marks)
(iii) not English;
(1 mark)
(iv) Irish, given that the player was a back; (2 marks)
(v) a forward, given that the player was not Scottish. (2 marks)
(b) Four players were selected at random from the squad to visit a school. Calculate the probability that all four players were English.

