

Statistics 1 Correlation and Regression Questions

- 1 At a certain small restaurant, the waiting time is defined as the time between sitting down at a table and a waiter first arriving at the table. This waiting time is dependent upon the number of other customers already seated in the restaurant.

Alex is a customer who visited the restaurant on 10 separate days. The table shows, for each of these days, the number, x , of customers already seated and his waiting time, y minutes.

x	9	3	4	10	8	12	7	11	2	6
y	11	6	5	11	9	13	9	12	4	7

- (a) Calculate the equation of the least squares regression line of y on x in the form $y = a + bx$.
(4 marks)
- (b) Give an interpretation, in context, for each of your values of a and b .
(2 marks)
- (c) Use your regression equation to estimate Alex's waiting time when the number of customers already seated in the restaurant is:
- (i) 5;
- (ii) 25. (2 marks)
- (d) Comment on the likely reliability of **each** of your estimates in part (c), given that, for the regression line calculated in part (a), the values of the 10 residuals lie between +1.1 minutes and -1.1 minutes. (3 marks)
-

5 [Figure 1, printed on the insert, is provided for use in this question.]

The table shows the times, in seconds, taken by a random sample of 10 boys from a junior swimming club to swim 50 metres freestyle and 50 metres backstroke.

Boy	A	B	C	D	E	F	G	H	I	J
Freestyle (x seconds)	30.2	32.8	25.1	31.8	31.2	35.6	32.4	38.0	36.1	34.1
Backstroke (y seconds)	33.5	35.4	37.4	27.2	34.7	38.2	37.7	41.4	42.3	38.4

(a) On **Figure 1**, complete the scatter diagram for these data. (2 marks)

(b) Hence:

(i) give **two** distinct comments on what your scatter diagram reveals; (2 marks)

(ii) state, **without calculation**, which of the following 3 values is most likely to be the value of the product moment correlation coefficient for the data in your scatter diagram.

0.912 0.088 0.462 (1 mark)

(c) In the sample of 10 boys, one boy is a junior-champion freestyle swimmer and one boy is a junior-champion backstroke swimmer.

Identify the **two** most likely boys. (2 marks)

(d) **Removing the data for the two boys whom you identified in part (c):**

(i) calculate the value of the product moment correlation coefficient for the remaining 8 pairs of values of x and y ; (3 marks)

(ii) comment, in context, on the value that you obtain. (1 mark)

- 1 The table shows, for each of a random sample of 8 paperback fiction books, the number of pages, x , and the recommended retail price, $\pounds y$, to the nearest 10p.

x	223	276	374	433	564	612	704	766
y	6.50	4.00	5.50	8.00	4.50	5.00	8.00	5.50

- (a) (i) Calculate the value of the product moment correlation coefficient between x and y . *(3 marks)*
- (ii) Interpret your value in the context of this question. *(2 marks)*
- (iii) Suggest one other variable, in addition to the number of pages, which may affect the recommended retail price of a paperback fiction book. *(1 mark)*
- (b) The same 8 books were later included in a book sale. The value of the product moment correlation coefficient between the number of pages and the sale price was 0.959, correct to three decimal places.

What can be concluded from this value? *(2 marks)*

- 3 A new car tyre is fitted to a wheel. The tyre is inflated to its recommended pressure of 265 kPa and the wheel left unused. At 3-month intervals thereafter, the tyre pressure is measured with the following results:

Time after fitting (x months)	0	3	6	9	12	15	18	21	24
Tyre pressure (y kPa)	265	250	240	235	225	215	210	195	180

- (a) (i) Calculate the equation of the least squares regression line of y on x . *(4 marks)*
- (ii) Interpret in context the value for the gradient of your line. *(2 marks)*
- (iii) Comment on the value for the intercept with the y -axis of your line. *(2 marks)*

- (b) The tyre manufacturer states that, when one of these new tyres is fitted to the wheel of a car and then inflated to 265 kPa, a suitable regression equation is of the form

$$y = 265 + bx$$

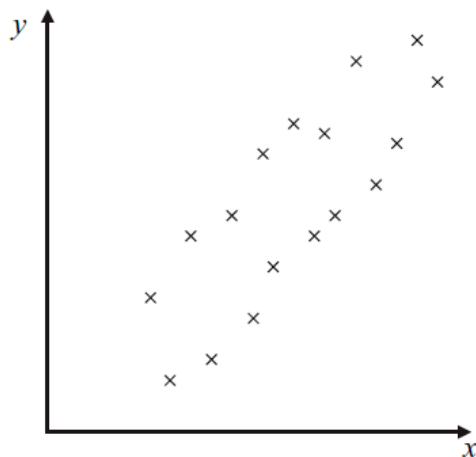
The manufacturer also states that, as the car is used, the tyre pressure will decrease at twice the rate of that found in part (a).

- (i) Suggest a suitable value for b . (2 marks)
- (ii) One of these new tyres is fitted to the wheel of a car and inflated to 265 kPa. The car is then used for 8 months, after which the tyre pressure is checked for the first time.

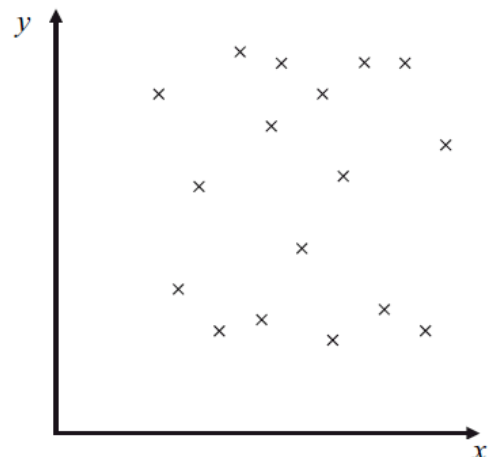
Show that, accepting the manufacturer's statements, the tyre pressure can be expected to have fallen below its minimum safety value of 220 kPa. (2 marks)

- 3 Estimate, **without undertaking any calculations**, the value of the product moment correlation coefficient between the variables x and y in each of the three scatter diagrams.

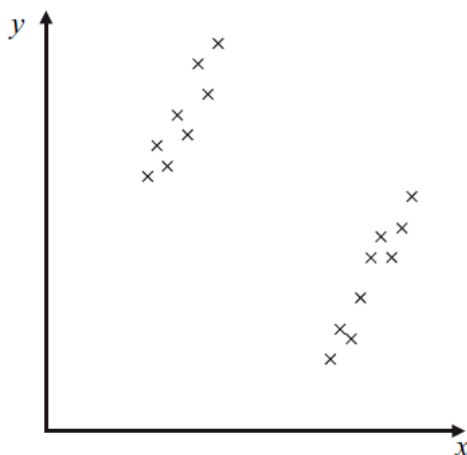
(a)



(b)



(c)



(5 marks)

7 [Figure 1, printed on the insert, is provided for use in this question.]

Stan is a retired academic who supplements his pension by mowing lawns for customers who live nearby.

As part of a review of his charges for this work, he measures the areas, $x \text{ m}^2$, of a random sample of eight of his customers' lawns and notes the times, y minutes, that it takes him to mow these lawns. His results are shown in the table.

Customer	A	B	C	D	E	F	G	H
x	360	140	860	600	1180	540	260	480
y	50	25	135	70	140	90	55	70

- (a) On **Figure 1**, plot a scatter diagram of these data. *(2 marks)*
- (b) Calculate the equation of the least squares regression line of y on x . Draw your line on **Figure 1**. *(6 marks)*
- (c) Calculate the value of the residual for Customer H and indicate how your value is confirmed by your scatter diagram. *(3 marks)*
- (d) Given that Stan charges £12 per hour, estimate the charge for mowing a customer's lawn that has an area of 560 m^2 . *(4 marks)*
-

1 The table shows the length, in centimetres, and maximum diameter, in centimetres, of each of 10 honeydew melons selected at random from those on display at a market stall.

Length	24	25	19	28	27	21	35	23	32	26
Maximum diameter	18	14	16	11	13	14	12	16	15	14

- (a) Calculate the value of the product moment correlation coefficient. *(3 marks)*
- (b) Interpret your value in the context of this question. *(2 marks)*
-

- 5 Bob, a gardener, measures the time taken, y minutes, for 60 grams of weedkiller pellets to dissolve in 10 litres of water at different set temperatures, x °C. His results are shown in the table.

x	16	20	24	28	32	36	40	44	48	52	56
y	4.7	4.3	3.8	3.5	3.0	2.7	2.4	2.0	1.8	1.6	1.1

- (a) State why the explanatory variable is temperature. *(1 mark)*
- (b) Calculate the equation of the least squares regression line $y = a + bx$. *(4 marks)*
- (c) (i) Interpret, in the context of this question, your value for b . *(2 marks)*
- (ii) Explain why no sensible practical interpretation can be given for your value of a . *(2 marks)*
- (d) (i) Estimate the time taken to dissolve 60 grams of weedkiller pellets in 10 litres of water at 30 °C. *(2 marks)*
- (ii) Show why the equation cannot be used to make a valid estimate of the time taken to dissolve 60 grams of weedkiller pellets in 10 litres of water at 75 °C. *(2 marks)*
-

Figure 1 (for use in Question 5)
Scatter Diagram for Freestyle and Backstroke Swimming Times

