

## Stats 2 Chi-Squared Contingency Table Tests Answers

| <b>2(a)</b> | $H_0$ : Choice independent of gender  | B1        |           | gender not associated with choice                                  |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
|-------------|---|-----------|-----------|--|---------|--------|---------|---------|--------|---------|---------|---------|--------|----------|---------|-------|----|--|--|
|             | <table style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th></th> <th>Squash</th> <th>Badminton</th> <th>Archery</th> <th>Hockey</th> </tr> </thead> <tbody> <tr> <td>Male</td> <td>5/3.5</td> <td>16/14</td> <td>30/24.5</td> <td>19/28</td> </tr> <tr> <td>Female</td> <td>4/5.5</td> <td>20/22</td> <td>33/38.5</td> <td>53/44</td> </tr> </tbody> </table> |           | Squash    | Badminton  | Archery | Hockey | Male    | 5/3.5   | 16/14  | 30/24.5 | 19/28   | Female  | 4/5.5  | 20/22    | 33/38.5 | 53/44 | M1 |  |  |
|             | Squash  | Badminton | Archery   | Hockey   |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
| Male        | 5/3.5   | 16/14     | 30/24.5   | 19/28  |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
| Female      | 4/5.5   | 20/22     | 33/38.5   | 53/44  |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
|             | Combine Squash and Badminton  | M1        |           | $E_i < 5$ (Similar categories)                                     |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
|             | <table style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th></th> <th>S &amp; B</th> <th>Archery</th> <th>Hockey</th> </tr> </thead> <tbody> <tr> <td>Male</td> <td>21/17.5</td> <td>30/24.5</td> <td>19/28</td> </tr> <tr> <td>Female</td> <td>24/27.5</td> <td>33/38.5</td> <td>53/44</td> </tr> </tbody> </table>   |           | S & B     | Archery  | Hockey  | Male   | 21/17.5 | 30/24.5 | 19/28  | Female  | 24/27.5 | 33/38.5 | 53/44  | M1<br>M1 |         |       |    |  |  |
|             | S & B   | Archery   | Hockey    |  |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
| Male        | 21/17.5   | 30/24.5   | 19/28     |  |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
| Female      | 24/27.5   | 33/38.5   | 53/44     |  |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
|             | $\chi^2$ values   |           |           |  |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
|             | <table style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th></th> <th>S &amp; B</th> <th>Archery</th> <th>Hockey</th> </tr> </thead> <tbody> <tr> <td>Male</td> <td>0.7000</td> <td>1.2347</td> <td>2.8928</td> </tr> <tr> <td>Female</td> <td>0.4455</td> <td>0.7857</td> <td>1.8409</td> </tr> </tbody> </table>   |           | S & B     | Archery  | Hockey  | Male   | 0.7000  | 1.2347  | 2.8928 | Female  | 0.4455  | 0.7857  | 1.8409 | M1       |         |       |    |  |  |
|             | S & B   | Archery   | Hockey    |  |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
| Male        | 0.7000  | 1.2347    | 2.8928    |  |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
| Female      | 0.4455  | 0.7857    | 1.8409    |  |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
|             | $\chi^2_{\text{calc}} = 7.90$   | A1        |           | (7.8 to 7.9)   |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
|             | $\nu = 2$   | B1        |           |  |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
|             | $\chi^2_{5\%}(2) = 5.991$   | B1ft      |           | (on their $\nu$ )  |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
|             | Reject $H_0$<br>Sufficient evidence, at the 1% level of significance, to support an association between the choice of sport and gender  | A1ft      | 10        | reject $H_0$ and $H_0$ stated<br><b>or</b><br>statement in context |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
| <b>(b)</b>  | <b>More females and fewer males</b> chose to participate in hockey <b>than expected</b>   | B1<br>B1  | 2         |  |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |
|             | <b>Total</b>  |           | <b>12</b> |  |         |        |         |         |        |         |         |         |        |          |         |       |    |  |  |

4(a)(i)

|       | A   | B  | Total |
|-------|-----|----|-------|
| 22-34 | 21  | 32 | 53    |
| 35-39 | 72  | 36 | 108   |
| 40-59 | 27  | 12 | 39    |
| Total | 120 | 80 | 200   |

B1  
B1

2

for A values  
for B values

(ii)

$H_0$  : no association between area  
and age profile  
 $H_1$  : association between area  
and age profile

B1

At least  $H_0$

| $O_i$            | $E_i$            | $\frac{(O_i - E_i)^2}{E_i}$ |
|------------------|------------------|-----------------------------|
| 24               | 31.8             | 3.6679                      |
| 72               | 64.8             | 0.8000                      |
| 24               | 23.4             | 0.5538                      |
| 32               | 21.2             | 5.5019                      |
| 36               | 43.2             | 1.2000                      |
| 12               | 15.6             | 0.8308                      |
| $\sum O_i = 200$ | $\sum E_i = 200$ | $\chi^2 = 12.554$           |

M1

M1

M1

M1

A1

B1

B1✓

Attempt at Row & Column totals  
Attempt at  $E_i$

Attempt at  $\frac{(O_i - E_i)^2}{E_i}$

Attempt at  $\chi^2$

AWFW 12.5 to 12.6 provided correct  
method used

$$\nu = (3-1)(2-1) = 2$$

$$\chi_{1\%}^2(2) = 9.210 < 12.554$$

Reject  $H_0$

The evidence suggests that the area within  
which a school is situated seems to have an  
effect on the age-profile of the staff  
employed.

E1✓

9

fit on  $\chi^2$  and calculated value  
depends on  $H_0$  correct, if stated

(b) There seems to be fewer staff employed in  
22 - 34 age group than expected in  
school A  
and more than expected in school B

E1

E1

2

**Total**

**13**

7(a)  $H_0$  : No association between the performances at KS3 and GCE

| $O_i$ | $E_i$ | $O_i - E_i$ | $X^2$  |
|-------|-------|-------------|--------|
| 60    | 63.55 | -3.55       | 0.1983 |
| 55    | 44.64 | 10.36       | 2.4043 |
| 40    | 46.81 | -6.81       | 0.9907 |
|       |       |             |        |
| 55    | 51.25 | 3.75        | 0.2744 |
| 32    | 36.00 | -4.00       | 0.4444 |
| 38    | 37.75 | 0.25        | 0.0017 |
|       |       |             |        |
| 47    | 46.33 | 0.67        | 0.0097 |
| 31    | 32.54 | -1.54       | 0.0733 |
| 35    | 34.13 | 0.87        | 0.0222 |
|       |       |             |        |
| 43    | 43.87 | -0.87       | 0.0173 |
| 26    | 30.82 | -4.82       | 0.7527 |
| 38    | 32.31 | 5.69        | 1.0005 |

$$X^2 = 6.1897$$

$$\nu = 3 \times 2 = 6 \Rightarrow \chi_{90\%}^2 = 10.645$$

Do not reject  $H_0$   
 No evidence to suggest an association between KS3 results and GCE grades at 10% level of significance.

(b) More of the students achieving level 7 at KS3 gain grade A's at GCE than expected.

B1

M1

M1

M1

M1

A1

B1B1✓

E1✓

E1

**Total**

$E_i$

$O_i - E_i$

$(O_i - E_i)^2 / E_i$

$\Sigma$

AWFW 6.05 – 6.35

on their  $\nu$

9

1

**10**

| <p><b>1</b> <math>H_0</math>: condition independent of treatment<br/> <math>H_1</math>: condition dependent upon treatment</p> <p>Totals: 66, 84, 75, 75</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th><math>O</math></th> <th><math>E</math></th> <th><math> O - E  - 0.5</math></th> <th><math>\frac{( O - E  - 0.5)^2}{E}</math></th> </tr> </thead> <tbody> <tr> <td>20</td> <td>33</td> <td>12.5</td> <td>4.7348</td> </tr> <tr> <td>55</td> <td>42</td> <td></td> <td>3.7202</td> </tr> <tr> <td>46</td> <td>33</td> <td></td> <td>4.7348</td> </tr> <tr> <td>29</td> <td>42</td> <td></td> <td>3.7202</td> </tr> </tbody> </table> <p><math>\chi^2 = 16.91</math></p> <p><math>\chi^2_{5\%}(1) = 3.841 &lt; 16.91</math><br/> Reject <math>H_0</math></p> <p>Evidence to suggest that the condition of the patients may be dependent upon the treatment that they received</p> | $O$          | $E$ | $ O - E  - 0.5$ | $\frac{( O - E  - 0.5)^2}{E}$ | 20 | 33 | 12.5 | 4.7348 | 55 | 42 |  | 3.7202 | 46 | 33 |  | 4.7348 | 29 | 42 |  | 3.7202 | <p>B1</p> <p>B1</p> <p>M1A1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>B1✓</p> <p>A1✓</p> <p>E1✓</p> | <p>for <math>E_i</math> attempted, correctly</p> <p>for use of Yates' correction</p> <p>final column</p> <p>allow 16.9<br/> If no Yates' correction:<br/> possible M1A1M0M1A0<br/> If 0.5 incorrectly used:<br/> possible M1A1M1M1A0</p> <p>for <math>\chi^2</math> on their <math>\nu</math><br/> iff <math>H_0</math> stated correctly<br/> dependent on third M1</p> | <p><b>10</b></p> |
|--|--------------|-----|-----------------|-------------------------------|----|----|------|--------|----|----|--|--------|----|----|--|--------|----|----|--|--------|--|---|------------------|
|  | $O$          | $E$ | $ O - E  - 0.5$ | $\frac{( O - E  - 0.5)^2}{E}$ |    |    |      |        |    |    |  |        |    |    |  |        |    |    |  |        |  |   |                  |
|  | 20           | 33  | 12.5            | 4.7348                        |    |    |      |        |    |    |  |        |    |    |  |        |    |    |  |        |  |   |                  |
|  | 55           | 42  |                 | 3.7202                        |    |    |      |        |    |    |  |        |    |    |  |        |    |    |  |        |  |   |                  |
|  | 46           | 33  |                 | 4.7348                        |    |    |      |        |    |    |  |        |    |    |  |        |    |    |  |        |  |   |                  |
|  | 29           | 42  |                 | 3.7202                        |    |    |      |        |    |    |  |        |    |    |  |        |    |    |  |        |  |   |                  |
|  | <b>Total</b> |     |                 | <b>10</b>                     |    |    |      |        |    |    |  |        |    |    |  |        |    |    |  |        |  |   |                  |