

4.

Figure 1

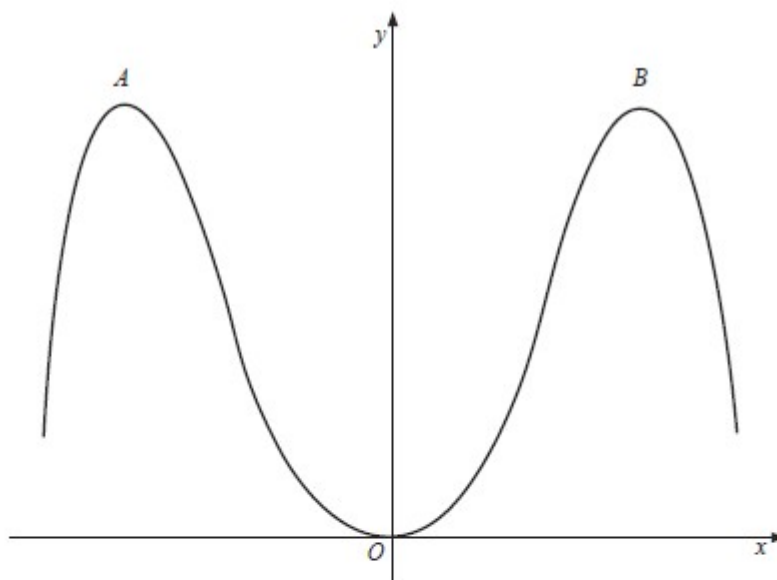


Figure 1 shows a sketch of the curve C with equation

$$y = \cos x \ln(\sec x), \quad -\frac{\pi}{2} < x < \frac{\pi}{2}.$$

The points A and B are maximum points on C .

(a) Find the coordinates of B in terms of e .

(5)

The finite region R lies between C and the line AB .

(b) Show that the area of R is

$$\frac{2}{e} \arccos\left(\frac{1}{e}\right) + 2 \ln\left(e + \sqrt{e^2 - 1}\right) - \frac{4}{e} \sqrt{e^2 - 1}.$$

[$\arccos x$ is an alternative notation for $\cos^{-1}x$]

(8)