3. A sequence $\{u_n\}$ is given by

$$\begin{aligned} u_1 &= k \\ u_{2n} &= u_{2n-1} \times p & n \geqslant 1 \\ u_{2n+1} &= u_{2n} \times q & n \geqslant 1 \end{aligned}$$

where k, p and q are positive constants with $pq \neq 1$

(a) Write down the first 6 terms of this sequence.

(b) Show that
$$\sum_{r=1}^{2n} u_r = \frac{k(1+p)(1-(pq)^n)}{1-pq}$$
 (6)

(3)

In part (c) [x] means the integer part of x, so for example [2.73] = 2, [4] = 4 and [0] = 0

(c) Find
$$\sum_{r=1}^{\infty} 6 \times \left(\frac{4}{3}\right)^{\left[\frac{r}{2}\right]} \times \left(\frac{3}{5}\right)^{\left[\frac{r-1}{2}\right]}$$
 (4)