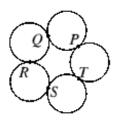




14. Five touching circles each have radius 1 and their centres are at the vertices of a regular pentagon. What is the radius of the circle through the points of contact *P*, *Q*, *R*, *S* and *T*?

A tan 18° B tan 36° C tan 45° D tan 54° E tan 72°



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14. **D** The internal angle of a regular pentagon is  $108^{\circ}$ . Let *A* be the centre of a touching circle, as shown. Since *OA* bisects  $\angle RAQ$ ,  $\angle OAQ = 54^{\circ}$ . Also, triangle *OAQ* is right-angled at *Q* (radius perpendicular to tangent). Since AQ = 1,  $OQ = \tan 54^{\circ}$ .

