



Suppose that  $x - \frac{1}{x} = y - \frac{1}{y}$  and  $x \neq y$ . What is the value of xy?

A 4

B 1 C -1 D -4 E more information is needed

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13. C  $x - \frac{1}{x} = y - \frac{1}{y}$  hence  $x^2y - y = xy^2 - x$ . Thus xy(y - x) + y - x = 0. Therefore (y - x)(xy + 1) = 0. As  $x \neq y$  then  $y - x \neq 0$ . Hence xy + 1 = 0 giving xy = -1.