



- 17. A solid cube is divided into two pieces by a single rectangular cut. As a result, the total surface area increases by a fraction f of the surface area of the original cube. What is the greatest possible value of f?
- A  $\frac{1}{3}$  B  $\frac{\sqrt{3}}{4}$  C  $\frac{\sqrt{2}}{3}$  D  $\frac{1}{2}$  E  $\frac{1}{\sqrt{3}}$

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The greatest possible value of f is achieved by a rectangular cut through an edge of a 17. cube and the furthest edge from it. If we take x as the side of the cube, by Pythagoras' Theorem the extra surface area formed by the cut is  $2\sqrt{2}x^2$ . Hence  $f = \frac{2\sqrt{2}x^2}{6x^2} = \frac{\sqrt{2}}{3}$ .